



# Comparative Analysis of Stochastics Approaches in Forecasting Nigeria's Key Macroeconomic Indicators

Dariyem Naandi Kruslat <sup>a,b,++\*</sup>, Waheed B. Yahya <sup>c</sup>  
and Msugh Moses Kembe <sup>d</sup>

<sup>a</sup> National Institute for Policy and Strategic Studies, Kuru, Nigeria.

<sup>b</sup> Department of Statistics, Nasarawa State University, Keffi, Nigeria.

<sup>c</sup> Department of Statistics, University of Ilorin, Kwara State, Nigeria.

<sup>d</sup> Department of Mathematics and Computer Science, Benue State University, Makurdi, Nigeria.

## Authors' contributions

This work was carried out in collaboration among all authors. All authors read and approved the final manuscript.

## Article Information

DOI: <https://doi.org/10.9734/ajpas/2024/v26i12682>

## Open Peer Review History:

This journal follows the Advanced Open Peer Review policy. Identity of the Reviewers, Editor(s) and additional Reviewers, peer review comments, different versions of the manuscript, comments of the editors, etc are available here: <https://www.sdiarticle5.com/review-history/127333>

Received: 20/09/2024

Accepted: 26/11/2024

Published: 03/12/2024

Original Research Article

## Abstract

The Nigerian economy faces significant volatility in key macroeconomic variables, posing challenges to economic stability and growth. This study compares the performance of ARIMA, GARCH, and VAR models in forecasting GDP, exchange rates, interest rates, inflation, and unemployment, using annual data from 1981-2024. Results show that while ARIMA and GARCH models capture certain dynamics, the VAR model consistently delivers the highest forecast accuracy across all variables. These findings offer valuable insights for policymakers seeking data-driven strategies to stabilize the economy and manage macroeconomic uncertainty.

<sup>++</sup> Research Directorate;

\*Corresponding author: Email: [naandikruslat2@gmail.com](mailto:naandikruslat2@gmail.com);

Cite as: Kruslat, Dariyem Naandi, Waheed B. Yahya, and Msugh Moses Kembe. 2024. "Comparative Analysis of Stochastics Approaches in Forecasting Nigeria's Key Macroeconomic Indicators". Asian Journal of Probability and Statistics 26 (12):38-50. <https://doi.org/10.9734/ajpas/2024/v26i12682>.

*Keywords: Stochastic modeling; vector autoregression (VAR); generalized autoregressive conditional heteroskedasticity (GARCH); autoregressive integrated moving average (ARIMA).*

## 1 Introduction

Macroeconomic stability is essential to economic growth, national wealth and development (Alwan, 2022; Kruslat et al., 2024). Evidence-based predictions and policies help to achieve sustainable growth. However, most economies globally continue to grapple with decades of instability across economic indicators (Adrangi and Kerr, 2022; Aizenman, 2020). The Nigerian economy, like many developing economies, is characterized by fluctuations in key macroeconomic variables such as GDP, inflation, interest rates, unemployment, and exchange rates. These fluctuations create challenges for policymakers in forecasting economic conditions and making informed decisions (Akpan, 2024; Onigah et al., 2024). Given the complex, volatile and non-linear nature of macroeconomic interactions, it is crucial to investigate and adopt robust models to better understand these dynamics (Kruslat et al., 2024).

The development and application of econometrical and statistical models are crucial for understanding economic behaviours and making informed policy decisions. These models facilitate the analysis of interdependences, predict complex behaviour and patterns within the macroeconomic ecosystem, contributing to economic stability and prosperity (Hrynychuk et al., 2022). Models serve as foundation for assessing economic relationships, allowing for evaluation of models based on data collections. Integrating statistical-econometric approaches enhances decision-making process, thereby ensuring models reflect the characteristics of economic phenomenon.

Stochastic time series modeling approaches like the Autoregressive Integrated Moving Average (ARIMA), Generalized Autoregressive Conditional Heteroskedasticity (GARCH), and Vector Autoregression (VAR) have been widely used to analyze the patterns and predict the future behaviours of such economic indicators (Hendikawati et al., 2020; Ezepue et al., 2022; Arumugam and Natarajan, 2023; Xuan et al., 2023; Sinu et al., 2024). They provide powerful tool for capturing the inherent uncertainties and volatility in macroeconomic variables. Each of these models has unique strengths in capturing different aspect of the times series data, ARIMA is well-suited for capturing linear trends and cyclical patterns, while GARCH is effective in modeling volatility, especially in financial time series. VAR, on the other hand, offers a comprehensive approach by analyzing the interrelationships among multiple variables, allowing for better policy simulation and economic forecasting but share commonalities in determining their predictive abilities on variables (Akkaya, 2021).

Over the years, economic forecasting often fails short in capturing the complexity and interrelationship of these variables, resulting to inadequate responses to economic shocks (Oyelami et al., 2016). Moreover, existing studies may not sufficiently address the stochastic nature of the Nigerian economy which is influenced by a variety of external and internal factors, including global economic conditions, political instability and local policy decisions (Markey-Towler, 2016).

The study aims to apply and compare ARIMA, GARCH, and VAR models to key macroeconomic variables in Nigeria to identify the most efficient for predictive purposes. By doing so, it seeks to provide valuable insight for policymakers in their effort to enhances economic stability and implement data driven macroeconomic interventions.

The primary objectives of the research are:

- i. To investigate the behaviour of key macromonomer variables using ARIMA, GARCH, and VAR models.
- ii. To compare the efficiency of the models under different conditions and identify the best the best-suited model for forecasting in the Nigerian context.

This study aim to fill the gap by employing some stochastic time series modeling processes; ARIMA, GARCH, and VAR to model key macroeconomic variables in Nigeria. By comparing the effectiveness of these models under varying conditions in predicting economic behaviours, this study provides valuable insight into their applicability and reliability in the Nigerian context. This contributes to the ongoing discourse on macroeconomic modeling in the Nigeria. It addresses current challenges within the system by offering empirical

analysis of these models and providing policy with evidence-based recommendations to manage macroeconomic uncertainties.

## 2 Literatures Review

Stochastic times series modeling is increasingly used in macroeconomics to understand the behaviours, complexity, volatility and non-linear interaction inherent in economic systems. By incorporating random shocks, these models provide a realistic representation of how unexpected events affect key economic variables like GDP and inflation. This approach helps policymakers understand risks better and craft more effective responses (Ezepue et al., 2022; Kruslat et al., 2024).

The study by Mohammed, examines the relationship between structure and behaviors in a macroeconomic model (Mohamed, 2011). Ding and Vo (2012) investigated the interactions between the oil market and the foreign exchange market using multivariate stochastic volatility (MSV) and multivariate GARCH (MGARCH) models, aiming to extract information from both markets for improved volatility forecasting. The study by Li et al., (2024) investigates the application of ARIMA and GARCH models to predict and analyze the fluctuations in the USD/EUR exchange rate over the next 53 weeks, using historical data from 2013 to 2023. The GARCH (1,1) model effectively analyzes volatility in finance, while the ARIMA model is not suitable for forecasting exchange rate fluctuation. Policymakers must prioritize addressing high inflation rates exchange rate and interest rate. Such rates can negatively impact purchasing power, external debt, fiscal deficit, exchange rates, interest rates, and investment (Okoye et al., 2019; Adeleye et al., 2019). Additionally, inflation models have been used to forecast crude oil reserves and production capacity in Nigeria (Kelechi et al., 2023).

Nigerian scholars often employ stochastic modeling to simulate the behavior of various macroeconomic variables, including GDP, inflation, interest rates, exchange rates, and unemployment, aiding policymakers in decision-making (Musa et al., 2021). Sovilj et al. (2023) argued that dynamic stochastic general equilibrium (DSGE) models have limitations in modeling and explaining real-world phenomena, particularly in relation to the recent (2007-2009) global financial crisis (Sovilj et al. 2023). Stochastics time-series modeling provides an important tool for better understanding economic variables and their analysing complex economic system by incorporating randomness and probability distribution into the model to better capture behaviors of economic variables and their interactions (Fajana and Adekoya, 2018; Zheng et al., 2020). Moreover, some models often struggle to fully encapsulate the inherent randomness and external shocks affecting macroeconomic variables, leading to potential inaccuracies in predictions (Li et al., 2024).

The application of stochastic time series modeling process helps researchers and policymakers better understand the potential outcomes of different economic policies under various scenarios, enabling the identification of effective policy interventions (Gbegbelegbe et al., 2019). Stochastics modeling processes is widely applied to analyse system volatility of and random system shocks (Ye and Xie, 2014; Hou and Zhang, 2020).

## 3 Methodology

The study applied a quantitative research design, applying a stochastic time-series approach to model and evaluate the predictive power of key macroeconomic variables. It analysed annul time series data from 1981 to 2023 on GDP, Exchange Rate (EXR), Interest rate (IR), Inflation rate (IFL), and Unemployment rate (UEMPL) as the key macroeconomic variables. The dataset was sourced from the CBN, NBS, and World Bank databases. To analyse the data, the researchers employed the R statistical software, specifically using the RStudio environment and EVIEW. These software packages were chosen for their robust statistical and econometric capabilities, allowing for comprehensive modeling and analysis.

### 3.1 Model specification

#### 3.1.1 Arima model

The ARIMA (AutoRegressive Integrated Moving Average) model is a robust time series forecasting method that effectively captures trends and patterns in non-stationary data. The ARIMA model was initially introduced in 1976 by George Box and Gwilym Jenkins, is characterized by linearity, combines Autoregressive (AR) and

Moving Average (MA) components, and is known for its highly accurate short-term forecasting precision (Xuan et al., 2023). Its components autoregression, differencing, and moving averages work together to provide accurate predictions across various fields, including economics and finance. The general form of the ARIMA model  $(p, d, q)$   $(P, D, Q)^L$ .

ARMA(p,q) Process

If we let  $\epsilon_1, \epsilon_2, \epsilon_3, \dots$  be a WhiteNoise  $(0, \theta_\epsilon^2)$  Process. It is defined that

$Y_1, Y_2, Y_3, \dots$  is an ARM  $(p, q)$  process if for some constant parameters

$\mu, \phi_1, \dots, \phi_p, \theta_1, \theta_2, \dots, \theta_q \in \mathbb{R}$

$$Y_t - \mu = \phi_1(Y_{t-1} - \mu) + \dots + \phi_p(Y_{t-p} - \mu) + \epsilon_t - \theta_1\epsilon_{t-1} - \dots - \theta_q\epsilon_{t-q} \quad (3.1)$$

ARIMA  $(p, d, q)$

A time series  $X_t$  is said to be an autoregressive integrated moving average process if  $\Delta^d X_t$

Is an ARIMA  $(p, d, q)$  process:

- i. Difference  $X_t$   $d$  times to achieve stationarity
- ii. Model  $Y_t = \Delta^d X_t$  as an ARMA  $(p, q)$  process
- iii. Integrate  $Y_t$   $d$  times to create a model for  $X_t$

$$Y_t = \frac{\theta_Q \beta \theta_Q(\beta^L)}{\phi_p(\beta) \theta_p(\beta) (1-\beta)^d (\beta)^d (1-\beta^L)^D} a_t \quad (3.2)$$

Where:

$$\beta \text{ is the backshift operator } (\beta_{yt} = y_{t-1}) \text{ Autogressive polynomial} \quad (3.3)$$

$\phi_p(\beta) = 1 - \phi_1\beta - \phi_2\beta^2 - \dots - \phi_p\beta^p$  is the coefficient of the non-seasonal AR component with degree of  $p$

$\theta_q(\beta) = 1 + \theta_1\beta + \theta_2\beta^2 + \dots + \theta_q\beta^q$  is the coefficient of the non-seasonal MA component with degree of  $q$

$\phi_p(\beta^L) = 1 - \phi_1\beta^L - \phi_2\beta^{2L} - \dots - \phi_p\beta^{pL}$  is the coefficient of the seasonal AR component with degree of  $p$

$\theta_Q(\beta) = (1 - \theta_1\beta^L - \theta_2\beta^{2L} - \dots - \theta_p\beta^{pL})$  is the coefficient of the seasonal with a component with degree of  $Q$

$(1 - \beta)^d$  is the difference for the season order  $L$  with degree  $D$ ,  $a_t$  is the residual values at time  $t$  that satisfy the white noise assumption

$t=1, 2, \dots, n$ , with  $n$  being the number of observation (Xuan et al., 2023)

### 3.1.2 GARCH (generalized autoregressive conditional heteroskedasticity model)

The GARCH model is use to model and forecast volatility, the model is specify by  $(p,q)$  where  $p$  is the order of the GARCH terms and  $q$  is the order of the ARCH term. The GARCH model is an extension of the ARCH( $q$ ) model in which the  $p$  lags of the past conditional variance were added to the equation. The model allows for both Autoregressive and moving average in the heteroscedastic variance (Ezepue et al., 2022). The GARCH  $(p,q)$  model is given as:

Let  $\epsilon_t \sim \text{WhiteNoise}(0,1)$ . Let the process  $\partial_t$  is a generalized Auto-Regressive Heteroscedasticity  $p, q$  or GARCH( $p,q$ ) Process if;

$$y_t = \mu + \epsilon_t$$

$$\partial_t = \sigma_t \epsilon_t \tag{3.4}$$

$$\sigma_t^2 = \alpha_0 + \sum_{i=1}^q \alpha_i \partial_{t-i}^2 + \sum_{j=1}^p \beta_j \sigma_{t-j}^2 \tag{3.5}$$

Where:  $\alpha_0, \alpha_1, \dots, \alpha_q, \beta_1, \dots, \beta_p \geq 0, \&$

$$\sigma_t = \sqrt{\alpha_0 + \sum_{i=1}^q \alpha_i \partial_{t-i}^2 + \sum_{j=1}^p \beta_j \sigma_{t-j}^2} \tag{3.6}$$

Is the conditional Standard deviation of  $\partial_t$  given past values

$$\partial_{t-1}, \dots, \partial_{t-q}, \sigma_{t-1}, \dots, \sigma_{t-p}$$

Square both Side by (3.6)

$$\partial_t^2 = (\alpha_0 + \sum_{i=1}^q \alpha_i \partial_{t-i}^2 + \sum_{j=1}^p \beta_j \sigma_{t-j}^2) \epsilon_t^2 \tag{3.7}$$

$$\sigma_t = \sqrt{\alpha_0 + \sum_{i=1}^q \alpha_i \partial_{t-i}^2 + \sum_{j=1}^p \beta_j \sigma_{t-j}^2} \tag{3.8}$$

Feedback of  $\sigma_{t-1}$  values  $\sigma_t$  to have more persistent period of high/low conditional volatility

$\partial_t$  is weakly stationarity with mean 0

$\partial_t$  has zero autocorrelation

$\partial_t^2$  has the autocorrelation of an ARMA(p, q) process

$$\partial_t \text{ is a robust noise term with conditional heteroscedasty} \tag{3.9}$$

Where;  $\sigma_t^2$  is the conditional variance

$\epsilon_t$  is the error term

$z_t$  is the independent identical distribution

$\alpha_0, \alpha_i, \beta_0, \beta_j$  are parameters to be estimated

The parameters  $\alpha_0, \alpha_1, \beta_j \geq 0, \sigma_t^2$  is the conditional variance  $\alpha_0$  is the

constante term,  $\alpha_0$  and  $\beta_j$  are the coefficient of the ARCH and GARCH

term respectively,  $\epsilon_{t-1}^2$  and  $y_{t-1}^2$  are the square errors at lag t-1 and t-j respectively

The GARCH (p,q) with  $Z_i$  is a discrete times stochastics process defined as

$\epsilon_t = Z_t \sigma_t$  which is weakly stationary with

$E(\epsilon_t) = 0$  and

$$\text{VAR}(\epsilon_t) = \alpha_0 [1 - (\sum \alpha_i + \sum_{j=1}^q \beta_j)] \tag{3.10}$$

$\text{COV}(\epsilon_t, \epsilon_s) = 0$  for  $t \neq s$ , if and only if

$$\sum_{i=1}^p \alpha_i + \sum_{j=1}^q \beta_j < 1$$

( $\alpha_0 > 0$ )

The GARCH model conditional variance(h)/volatility at time t depend on both past values of the shocks capture by the logged square error terms  $\varepsilon^2_{i-1}$  and the past values of itself ( $\sigma^2_{t-1}$ ).

### 3.1.3 Vector autoregressive (VAR) model

The VAR model is use to determine the dynamic relationship among variables. Consider for structural model of large-scale simultaneous equation and important to make strong prediction (Akkaya, 2021). Vector Autoregression (VAR) model is a statistical model used to capture the linear interdependencies among multiple time series. Each variable in a VAR model is modeled as a linear function of its own past values and the past values of all other variables in the system. The specification can include multiple equations, enhancing the model's capacity to capture complex dynamics among variables (Aswini et al., 2018).

#### 3.1.3.1 Specification

$$\begin{aligned} GDP &= GDP_t \\ \text{Exchange rate} &= EXR_t \\ \text{Unemployment rate} &= UNEMP_t \\ \text{Interest rate} &= IR_t \\ \text{Infaltion} &= IFL_t \end{aligned}$$

$$X_t = \alpha + \sum_{i=1}^p A_i x_{t-1} + \varepsilon_t \tag{3.11}$$

The stochastic part  $x_t$  is assumed to be generated by VAR process of order p (VAR(p) of the form

$$X_t = A_1 x_{t-1} + A_2 x_{t-2} + \dots + A_p x_{t-p} + \varepsilon_t, \text{ where} \tag{3.12}$$

#### 3.1.3.2 Endogenous variables

The vector  $X_t$  contains the time series data for the k endogenous variables. For example, in a VAR model with GDP, Exchange Rate, Interest Rate, Inflation, and Unemployment,  $X_t$  would be:

$$X_t = \begin{pmatrix} GDP_t \\ EXR_t \\ UNEMP_t \\ IR_t \\ IFL_t \end{pmatrix} \text{ is the vector of the variables} \tag{3.13}$$

$A_1, A_2, \dots, A_3$  are the matrix of the coefficient that will be estimated

$$\varepsilon_t = \begin{pmatrix} \varepsilon_{GDP} \\ \varepsilon_{EXR} \\ \varepsilon_{UNEMP} \\ \varepsilon_{IR} \\ \varepsilon_{IFL} \end{pmatrix} \text{ is the vector of the error terms that are assume to be white noise}$$

$$\begin{bmatrix} X_{1t} \\ X_{2t} \\ X_{3t} \\ X_{4t} \\ X_{5t} \end{bmatrix} = \begin{bmatrix} c_1 \\ c_2 \\ c_3 \\ c_4 \\ c_5 \end{bmatrix} \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} \\ a_{51} & a_{52} & a_{53} & a_{54} & a_{55} \end{bmatrix} \begin{bmatrix} X_{1,t-1} \\ X_{2,t-1} \\ X_{3,t-1} \\ X_{4,t-1} \\ X_{5,t-1} \end{bmatrix} + \begin{bmatrix} \varepsilon_{1t} \\ \varepsilon_{2t} \\ \varepsilon_{3t} \\ \varepsilon_{4t} \\ \varepsilon_{5t} \end{bmatrix} \tag{3.14}$$

Individual Equations:

$$\begin{aligned} GDP_i &= a_{11}GDP_{t-1} + a_{12}EXR_{t-2} + a_{13}UNEMP_{t-3} + a_{14}IR_{t-4} + a_{15}IFR_{t-5} + \varepsilon_{GDP_i} \\ EXR_i &= a_{21}GDP_{t-1} + a_{22}EXR_{t-2} + a_{23}UNEMP_{t-3} + a_{24}IR_{t-4} + a_{25}IFR_{t-5} + \varepsilon_{EXR_i} \\ UNEMP_i &= a_{31}GDP_{t-1} + a_{32}EXR_{t-2} + a_{33}UNEMP_{t-3} + a_{34}IR_{t-4} + a_{35}IFR_{t-5} + \varepsilon_{UNEMP_i} \\ IR_i &= a_{41}GDP_{t-1} + a_{42}EXR_{t-2} + a_{43}UNEMP_{t-3} + a_{44}IR_{t-4} + a_{45}IFR_{t-5} + \varepsilon_{IR_i} \\ IFR_i &= a_{51}GDP_{t-1} + a_{52}EXR_{t-2} + a_{53}UNEMP_{t-3} + a_{54}IR_{t-4} + a_{55}IFR_{t-5} + \varepsilon_{IFR_i} \end{aligned}$$

where  $a_{ij}$  are the coefficient estimate

### 3.1.4 Model evaluation criteria

Forecasting the performance of various forecasting model is essential in selecting best accuracy model, the Mean Absolute Error (MAE), Root Mean Square Error (RMSE) and Mean absolute percentage error. Reliability testing of the models is crucial to assess and validate their performance within the system. This process ensures that the model metrics, which are integral to determining the accuracy of the series ratios, reflect the true performance of the forecast ratios based on the model itself. To evaluate and validate the models used in this study, error metrics are employed, including Root Mean Squared Error (RMSE), Mean Absolute Error (MAE), and Thiel's Inequality Coefficient. RMSE is widely recognized as a robust metric for measuring a model's error in predicting quantitative data, as it calculates the standard deviation of the mean residual and then takes the square root of that mean. In contrast, MAE offers a simpler measure of forecast accuracy by using the absolute residual values. Both metrics provide insights into the model's performance, with RMSE focusing on the variance of errors and MAE on the average magnitude of errors.

The forecast evaluation metrics used in this study are mean absolute error (MAE) is defined as:

$$MEA = \frac{1}{n} \sum_{t=1}^n [r^2_t - \sigma^2_t] \quad (3.15)$$

The Root Mean Square Forecast Error (RMSE) is defined as:

$$RMSE = \sqrt{\frac{1}{n} \sum_{t=1}^n (r^2_t - \sigma^2_t)} \quad (3.16)$$

The  $r^2$  is the realised or actual variance and  $\sigma^2$ , is the square root of the conditional forecast variance and n is the number of fitted parameter (Isah et al., 2015)

and the Mean Absolute Percentage Error is defined as

$$MAP= = \frac{1}{n} \sum_{t=1}^n \left| \frac{(r_t - \sigma_t)}{r_t} \right| \quad (3.17)$$

where the actual and predicted values for corresponding  $t$  values are denoted by  $r_t$  and  $\sigma_t$  respectively.

### 3.1.5 Thiel's inequality coefficient

The Theil Inequality Coefficient (U) is a measure of the accuracy of a forecasting model. It compares the forecasted values to the actual values, where a value of 0 indicates a perfect forecast and values closer to 1 indicate worse performance.

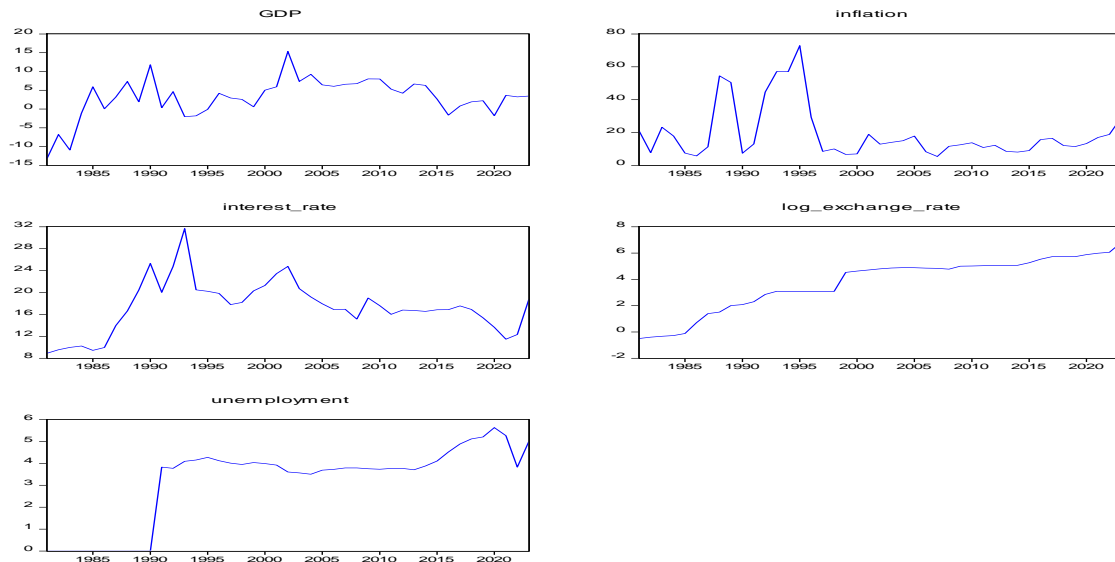
The model specification is given as:

$$U = \frac{\sqrt{\frac{1}{n} \sum_{t=1}^n (r^2_t - \sigma^2_t)}}{\sqrt{\frac{1}{n} \sum_{t=1}^n r^2_t + \sqrt{\frac{1}{n} \sum_{t=1}^n \sigma^2_t}}} \quad (3.18)$$

Where:

- $r^2_t$  is the forecasted value at time t
- $\sigma^2_t$  is the actual value at time t
- n is the number of observations
- The numerator  $\sqrt{\frac{1}{n} \sum_{t=1}^n (r^2_t - \sigma^2_t)}$  represents the Root Mean Squared Error (RMSE) between the forecasted and actual values.
- The denominator is the sum of the root mean squares of the forecasted and actual values, providing a normalization factor to ensure that the coefficient is between 0 and 1.

## 4 Main Results and Discussion



**Fig. 1. Time Series Plot of key Macroeconomic Variables Over 1981 to 2023 Period**

The graph in Fig. 1, shows the trends of key macroeconomic variables in Nigeria from 1981 to 2023, It illustrates the dynamic and volatile nature of Nigeria's key macroeconomic variables: GDP, inflation, interest rate, exchange rate, and unemployment, each exhibiting significant fluctuations and trends. The data shows high volatility and uncertainty across all macroeconomic variables.

### 4.1 Empirical analysis of the stochastic time series process using ARIMA, GARCH, and VAR models

The Autoregressive Integrated Moving Average (ARIMA) model, denoted as ARIMA (p, d, q), captures both linear and non-linear relationships among macroeconomic variables, making it a robust tool for time series analysis (Wang et al., 2021). In this study, key macroeconomic indicators, including GDP, inflation, interest rates, unemployment, and exchange rates, were modeled using ARIMA techniques. The dataset was partitioned into training (80%) and testing (20%) sets for effective model evaluation.

**Table 1. Summary of fit ARIMA model**

Series	GDP	Exchange Rate	Interest Rate	Inflation	Unemployment
ARIMA Model	(1,1,0)	(0,1,0)	(1,0,0)	(0,0,1)	(0,1,0)
Coefficients					
Ma	-0.515	0.1734	0.803	0.738	
s.e.	0.150	0.0445	0.103	0.097	
sigma <sup>2</sup>	18.91	0.0852	10.080	0.5491	0.455
log likelihood	-94.96	-7.38	-87.02	-111.34	-33.85
AIC	193.93	18.76	180.04	229.08	69.69
BIC	196.92	22.24	184.61	239.05	71.19

The ARIMA models fitted to GDP, Exchange Rate, Interest Rate, Inflation, and Unemployment reveal varying levels of model fit. The Exchange Rate model, an ARIMA (0,1,0), demonstrates the best fit with the lowest AIC and BIC values, indicating it effectively captures the series' dynamics as a random walk. In contrast, the GDP model (ARIMA (1,1,0)) shows the poorest fit, with high residual variance and the highest AIC/BIC, suggesting it may not fully capture the complexities of GDP movements. The Interest Rate and Inflation models also fit reasonably well but exhibit some residual variability.



**Table 2. Training set error measure**

Measure	GDP	Exchange Rate	Interest Rate	Inflation	Unemployment
ME	0.5480	-1.5578	0.282	-0.0011	0.114
RMSE	4.0207	0.2857	3.080	0.7303	0.664
MAE	3.0365	0.1853	2.248	0.5631	0.174
MPE	-195.23	5.1353	-1.231	-6.6500	4.168
MAPE	7.2884	9.2524	12.557	20.923	6.443
MASE	0.8728	1.0329	1.013	0.5999	0.970

The training set error measures provide valuable insight into the performances of ARIMA models, with RMSE and MAPE revealing varying predictive accuracies across the macroeconomic variables. GDP’s RMSE of 4.02 indicates a moderate level of prediction error. The performances measurement errors for exchange rate, inflation and unemployment rate are also better.

#### 4.1.1 Generalized autoregressive conditional heteroskedasticity (GARCH)

The GARCH model was applied to capture the dynamic volatility and influence of macroeconomic variables on GDP. The GARCH model’s result reveal significant coefficients that signifies relationship between GDP and other key variables in the study.

**Table 3. GARCH model estimation results for GDP dynamics**

Variable	Coefficient	Std. Error	z-Statistic	Prob.
Inflation	-0.075415	0.032810	-2.298502	0.0215
Interest rate	0.494225	0.107573	4.594334	0.0000
Exchange rate	1.936157	0.552474	3.504523	0.0005
Unemployment	-2.198102	0.555234	-3.958877	0.0001
C	-3.490293	2.397591	-1.455750	0.1455

As seen in Table 3, the mean equation indicates that inflation negatively impact GDP, while interest rate and exchange rate positively influence GDP growth. Unemployment has a detrimental effect on GDP, emphasizing the importance of these variables in economic policy.

**Table 4. Evaluation of GARCH Models for Forecasting Key Macroeconomic Variables in Nigeria**

Criteria	GDP	Exchange Rate	Interest Rate	Inflation	Unemployment
Akaike	6.142	2.398	5.431	7.974	1.919
Bayesian	6.306	2.562	5.594	8.138	2.083
Shibata	6.122	2.383	5.450	7.951	1.902
Hannan-Quinn	6.203	2.459	5.491	8.035	1.979
RMSE	2.202	5.871	15.856	18.702	4.802

The GARCH model’s evaluation metrics demonstrated its predictive capability for GDP, exchange rate and unemployment rate, with lower RMSE values. This indicates better accuracy compared to inflation and interest rate, which showed higher prediction errors.

#### 4.2 Model evaluation and validation using the VAR model

**Table 5. Model evaluation**

Variable	RMSE	MAE	Theil’s inequality coefficient	Symmetric MAPE
GDP	1.054	0.79	0.337	67.0
Exchange Rate	0.350	0.309	0.049	5.22
Interest Rate	0.186	0.124	0.032	4.34
Inflation	0.543	0.415	0.096	14.2
Unemployment	0.321	0.217	0.110	10.1

The model evaluation result (Table 5) shows the performance metrics for; GDP, Exchange Rate, Interest Rate, Inflation, and Unemployment. The metrics used the Root Mean Square Error (RMSE), Mean Absolute Error (MAE), Theil's Inequality Coefficient, and Symmetric Mean Absolute Percentage Error (SMAPE). The Theil static statistics predictive model for GDP shows moderate errors, with RMSE of 1.054 and an MAE of 0.79, indicating relatively low prediction accuracy. The Theil's Inequality Coefficient of 0.337, which is less than 1, affirmed that the model has a good predictive power with insignificant inaccuracies. The moderate SMAPE of 67.0 indicates that the relative error in percentage terms is considerable, pointing to significant challenges in accurately predicting GDP. The VAR model performs well in predicting the exchange rate, with a low RMSE of 0.350 and MAE of 0.309, indicating an average prediction error. The Theil's Inequality Coefficient of 0.049 indicates a higher forecasting accuracy. Moreover, the low SMAPE of 5.22% further confirms the model's strong performance for exchange rate.

The prediction indices for interest rate also shows high accuracy, with a low RMSE of 0.186 and MAE of 0.124. The Theil's Inequality Coefficient of 0.032, indicating excellent predictive power. Low SMAPE of 4.34 % affirmed the model's accuracy in forecasting interest rate. On the same scale, inflation measurement shows moderate accuracy, with an RMSE of 0.543 and MAE of 0.415. The Theil's Inequality Coefficient of 0.096 implies significant predictive power. The SMAPE of 14.2 % indicates a moderate level of relative predictive error. The model's predictive power for unemployment is fairly accurate, with a RMSE of 0.321 and MAE of 0.217, indicating average prediction error. The Theil's Inequality Coefficient of 0.110 indicates good forecasting ability, and SMAPE of 10.1 % confirmed reliable model performance.

## 5 Discussion of Findings

The study presents an empirical insight into the performance of stochastic time series approaches to macroeconomic variables. It presents the comparative analysis of three statistical models: ARIMA, GARCH and VAR in forecasting key macroeconomic variables in Nigeria. The ARIMA, GARCH model, which incorporates both autoregressive integrated moving average (ARIMA) and generalized autoregressive conditional heteroskedasticity (GARCH) components, generally outperforms the GARCH model in terms of in-sample forecast accuracy, as evidenced by the lower RMSE, MAE, and MAPE values. This suggests that the ARIMA component effectively captures the linear dynamics of the variables, while the GARCH component adequately models the conditional heteroskedasticity.

Moreover, the VAR model demonstrate strong performance in forecasting the studied variables, compared to the other models. It exhibits low RMSE, MAE, Theil's inequality coefficient, and SMAPE values across all variables, indicating its accuracy and reliability. While ARIMA and GARCH models are effective in capturing certain forms of volatility in the Nigeria economy, the Var model is more capable in providing accurate forecast for the studied variables in the Nigeria economy. This reinforced the study by Taiwo *et al.*, asserted that the VAR model give a better forecast of macroeconomic data in Nigeria (Taiwo et al., 2022). Studies also reveal that the VAR model outperformed other traditional forecasting approaches in terms of accuracy (Chang et al., 2021; Hafner et al., 2021). This aligned with the studies by Ibrahim et al., and Yang *et al.* that VAR performance better compared to BVAR and ARIMA (Yang et al., 2020; Ibrahim et al., 2020). Making it suitable for forecasting time series model for policymakers making reliable forecast (Li et al., 2020; Tejesh and Khajabee, 2024). More so, it validates the model's ability to handle the interdependences between variables is a key advantage.

## 6 Conclusion

The findings of this study have important implications for the future study of macroeconomic variables in Nigeria. First, the comparative analysis demonstrates the importance of considering both linear and non-linear dynamics when modeling macroeconomic variables. The study provide insight into improving economic forecasting strategies for Nigeria, which is essential in formulating economic policies, making informs decisions that will address national challenges, better understanding and control of economic instabilities. The ARIMA-GARCH model's performance highlights the benefits of incorporating both components. The VAR model demonstrate strong performance in forecasting key macroeconomic variables in Nigeria. It outperformed others in terms of forecast accuracy and lower error rates, indicating its predictive power and reliability. Moreover, the study underscores the challenges associated with forecasting macroeconomic variables. Hence, undertaking this

predictive modeling, offers valuable insight into model's accuracy and effectiveness for economic forecasting which is critical for data-driving policy making

## Disclaimer (Artificial Intelligence)

Author(s) hereby declares that NO generative AI technologies such as Large Language Models (ChatGPT, COPILOT, etc.) and text-to-image generators have been used during the writing or editing of this manuscript.

## Competing Interests

Authors have declared that no competing interests exist.

## References

- Adeleye, N., Ogundipe, A. A., Ogundipe, O., Ogunrinola, I., & Adediran, O. (2019). Internal and external drivers of inflation in Nigeria. *Banks and Bank Systems*, 14(4), 206-218. [https://doi.org/10.21511/bbs.14\(4\).2019.19](https://doi.org/10.21511/bbs.14(4).2019.19)
- Adrangi, B., & Kerr, L. (2022). Sustainable development indicators and their relationship to GDP: Evidence from emerging economies. *Sustainability*, 14(658), 1-13. <https://doi.org/10.3390/su14020658>
- Aizenman, J. (2020). Macroeconomic challenges and the resilience of emerging market economies in the 21st century (ADBI Working Paper 1131). Asian Development Bank Institute. <https://www.adb.org/publications/macroeconomic-challenges-resilience-emerging-market-economies-21st-century>
- Akkaya, M. (2021). Vector autoregressive model and analysis. [https://doi.org/10.1007/978-3-030-54108-8\\_8](https://doi.org/10.1007/978-3-030-54108-8_8)
- Akpan, J. E. (2024). Econometric analysis of inflation and monetary policy indices in Nigeria. *Gusau Journal of Economics and Development Studies*, 4(1), 53–65. <https://doi.org/10.57233/gujeds.v4i1.4>
- Alwan, G. H. (2022). Analyzing the causal relationship between the variables of economic stability in Iraq using Granger's causality. *Estudios de economía aplicada*, 40(3). <https://doi.org/10.25115/eea.v40i3.7023>
- Arumugam, V., & Natarajan, V. (2023). Time series modeling and forecasting using autoregressive integrated moving average and seasonal autoregressive integrated moving average models. *Instrumentation Mesure Métrologie*, 22(4), 161-168. <https://doi.org/10.18280/i2m.220404>
- Aswini, K., Mani, C., Srivyshnavi, P., Venkata, S., Ramaraju, R., Ramanjuneyulu, B., Mokesh, G., & Balasiddamuni, P. (2018). Specification and stability of two equations vector autoregressive model for time series data analysis. *International Journal of Statistics and Applied Mathematics*, 3(2), 538-548.
- Chang, C. L., McAleer, M., & Wang, Y. A. (2021). Forecasting cryptocurrency prices using vector autoregression models. *Journal of Forecasting*, 40(1), 77-91.
- Ding, L., & Vo, M. (2012). Exchange rates and oil prices: A multivariate stochastic volatility analysis. *The Quarterly Review of Economics and Finance*, 52(1), 15–37. <https://doi.org/10.1016/j.qref.2012.01.003>
- Ezepue, P. O., Omar, M. T., & Babayemi, A. (2022). Stochastic modelling in financial markets: Case study of the Nigerian stock market.
- Fajana, O. O., & Adekoya, O. A. (2018). An assessment of system dynamics simulation for policy analysis in Nigeria. *International Journal of Engineering and Technology (UAE)*, 7(4.11), 238–245.
- Gbegbelegbe, S., Msangi, S., De Pinto, A., Robertson, R., & Nkonya, E. (2019). The use of system dynamics for policy analysis of food security in sub-Saharan Africa: A review. *Agricultural Systems*, 176, 102657.

- Hafner, C. M., Herwartz, H., & Stöver, B. (2021). Bitcoin price forecasting with a VAR model incorporating data from Google Trends and gold prices. *Journal of Forecasting*, 40(4), 576-588.
- Hendikawati, P., Subanar, A., Abdurakhma, & Tarno. (2020). A survey of time series forecasting from stochastic methods to soft computing. *Journal of Physics: Conference Series*, 1613(1), 012019. <https://doi.org/10.1088/1742-6596/1613/1/012019>
- Hou, D., & Zhang, Y. (2020). Stochastic modeling and optimization in engineering. John Wiley & Sons.
- Hrynchuk, T., Hulivata, I., & Husak, L. (2022). The significance of econometric models in the process of forecasting economic indicators. *SSRN*. <https://doi.org/10.2139/ssrn.4227114>
- Ibrahim, A., Rasha, K., Menglu, L., Esteban, V., & Eric, H. (2020). Bitcoin network mechanics: Forecasting the BTC closing price using vector auto-regression models based on endogenous and exogenous feature variables. *Journal of Risk and Financial Management*, 13(9), 189. <https://doi.org/10.3390/jrfm13090189>
- Isah, A., Dikko, H. G., & Chinyere, E. S. (2015). Modeling the impact of crude oil price shocks on some macroeconomic variables in Nigeria using GARCH and VAR models. *American Journal of Theoretical and Applied Statistics*, 4(5), 359-367. <https://doi.org/10.11648/j.ajtas.20150405.16>
- Kelechi, A. C., Chinenye, A. C., & Emmanuel, E. C. (2023). Modeling and forecasting of Nigeria crude oil production. *Journal of Mathematics and Statistics Studies*, 4(1), 58-67. <https://doi.org/10.32996/jmss>
- Kruslat, N. D., Kembe, M. M., Garba, G., & Sulaiman, I. (2024). Review on system dynamics modeling approach to macroeconomic variables in Nigeria. *International Journal of Advanced Research in Multidisciplinary Studies (IJARMS)*, 4(1), 367-377.
- Kruslat, N. D., Kembe, M. M., Yahya, W. B., & Umar, I. M. (2024). Stochastic modeling of key macroeconomic variables in Nigeria. *International Journal of Research Publication and Reviews*, 5(8), 2242-2250.
- Li, J., & Li, Y. (2020). Forecasting cryptocurrency prices using VAR models. *Journal of Risk and Financial Management*, 13(12), 299.
- Li, J., Yin, J., & Zhang, R. (2024). Analysis and forecast of USD/EUR exchange rate based on ARIMA and GARCH models. *Applied Economics and Policy Studies*, 566-575. [https://doi.org/10.1007/978-981-97-0523-8\\_54](https://doi.org/10.1007/978-981-97-0523-8_54)
- Markey-Towler, B. (2016). Principles of forecasting in complex economic systems. *SSRN*. <https://doi.org/10.2139/ssrn.2907197>
- Mohamed, I. A. W. (2011). Applying system dynamic model for macroeconomic analysis of Yemen. *Econometrics, Mathematical Methods and Programming Journal*, 4(38). <https://ssrn.com/abstract=1825905>
- Musa, H. I., Idris, M. A., & Abdulrahman, S. S. (2021). Evaluating the impact of monetary policy on the Nigerian economy using stochastic modeling. *Journal of Business and Economic Development*, 6(1), 44-53.
- Okoye, U. L., Olokoyo, F. O., Ezeji, F. N., Okoh, J. I., & Evbuomwan, G. O. (2019). Determinants of behavior of inflation rate in Nigeria. *Investment Management and Financial Innovations*, 16(2), 25-36. [https://doi.org/10.21511/imfi.16\(2\).2019](https://doi.org/10.21511/imfi.16(2).2019)
- Onigah, P. O., Onwumere, J. U., Kalu, E. U., Emori, E. G., Ahakiri, F. I., & Ukpere, W. I. (2024). Effect of selected macroeconomic variables on external reserves management in Nigeria (1981-2022). *Educational Administration: Theory and Practice*, 30(5), 13787-13799. <https://doi.org/10.53555/kuey.v30i5.6039>

- Oyelami, L. O., Olomola, P. A., & Camarero, M. (2016). External shocks and macroeconomic responses in Nigeria: A global VAR approach. *Cogent Economics & Finance*, 4(1). <https://doi.org/10.1080/23322039.2016.1239317>
- Sinu, E. B., Kleden, M. A., & Atti, A. (2024). Application of ARIMA model for forecasting national economic growth: A focus on gross domestic product data. *BAREKENG: Journal of Mathematics & Its Application*, 18(2), 1261-1272.
- Sovilj, S., Tkalec, M., Pripuzić, D., & Kostanjčar, Z. (2023). Modelling national economic system: A case of the Croatian economy. *South East European Journal of Economics and Business*, 18(1), 115-144. <https://doi.org/10.2478/jeb-2023-0009>
- Taiwo, A. I., Oyewole, P., & Dehinsilu, O. A. (2022). Modelling and forecasting Nigerian macro-economic variables with multiple time series model. *FUW Trends in Science & Technology Journal*, 7(1), 017–023.
- Tejesh, H. R., & Khajabee, M. (2024). Dynamic interaction among selected world stock indices: A VAR approach. *Theoretical and Applied Economics*, 21(3), 227-242.
- Wang, H., Yang, M., He, R., & Zheng, P. (2021). Environmental regulation, foreign direct investment, and export sophistication of China: An empirical study based on dynamic system GMM and threshold model. *Environmental Science and Pollution Research*. <https://doi.org/10.1007/s11356-021-14833-2>
- Xuan, H., Maestrini, L., Chen, F., & Grazian, C. (2023). Stochastic variation inference for GARCH model. *Springer Nature*.
- Yang, L., Zhang, Q., Zhang, C., & Du, R. (2020). Forecasting cryptocurrency prices using a VAR model. *Mathematics*, 8(12), 2140.
- Ye, Z.-S., & Xie, M. (2014). Stochastic modelling and analysis of degradation for highly reliable products. *Applied Stochastic Models in Business and Industry*, 31(1), 16–32. <https://doi.org/10.1002/asmb.2063>
- Zheng, J., Li, D., Li, Y., Chen, J., & Zheng, W. (2020). Dynamic stochastic modeling for transport system operation: A review. *IEEE Access*, 8, 136928–136941.

**Disclaimer/Publisher's Note:** The statements, opinions and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of the publisher and/or the editor(s). This publisher and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions or products referred to in the content.

© Copyright (2024): Author(s). The licensee is the journal publisher. This is an Open Access article distributed under the terms of the Creative Commons Attribution License (<http://creativecommons.org/licenses/by/4.0>), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

**Peer-review history:**

The peer review history for this paper can be accessed here (Please copy paste the total link in your browser address bar)

<https://www.sdiarticle5.com/review-history/127333>