

British Journal of Applied Science & Technology 4(29): 4136-4147, 2014



SCIENCEDOMAIN international www.sciencedomain.org

# **Characteristics of Non-spinning Black Holes**

# Dipo Mahto<sup>1\*</sup>, Brajesh Kumar Jha<sup>2</sup>, Murlidhar Prasad Singh<sup>3</sup> and Promod Jha<sup>4</sup>

<sup>1</sup>Department of Physics, Marwari College, T.M.B.U., Bhagalpur, India. <sup>2</sup>University Department of Physics, L.N.M.U., Darbhanga, India. <sup>3</sup>Department of Physics, B.N.M. College, Barhiya, T.M.B.U., Bhagalpur, India. <sup>4</sup>Department of Physics, C.M. Science College, L.N.M.U., Darbhanga, India.

# Authors' contributions

This study was carried out in collaboration among all the authors. Author DM collected and prepared the paper with calculations and wrote the first draft of the manuscript. Author BKJ designed the study and contributed to the statistical analysis. Author MPS plotted the graphs and gave some statistical analysis. Author PJ supervised the whole study. All authors read and approved the final manuscript.

**Original Research Article** 

Received 20<sup>th</sup> May 2014 Accepted 3<sup>rd</sup> July 2014 Published 1<sup>st</sup> August 2014

# ABSTRACT

**Aims:** To derive an expression for the wavelength/frequency of Hawking radiation emitted by non-spinning black holes in terms of the radius of event horizon ( $\lambda = 8\pi R_s \& v = c/8\pi R_s$ ) using quantum theory of radiation (E = hv) energy of Hawking radiation and the radius of event horizon of non-spinning black holes ( $R_s = 2GM/c^2$ ), which may be regarded as the characteristics of non-spinning black holes.

**Study Design:** Data for the frequencies and wavelengths of Hawking radiation emitted from black holes have been calculated with the help of rest masses for stellar – mass black holes (M ~ 5 - 20 M<sub>☉</sub>) in X-ray binaries and for the super massive black holes (M ~  $10^6 - 10^{9.5} M_{\odot}$ ) in active galactic nuclei using  $\lambda = 8\pi R_s$  &  $v = c/8\pi R_s$  which corresponds to the research work entitled: Frequency of Hawking radiation from black holes by Mahto et al. in International Journal of Astrophysics and Space Science (Dec. 2013).

**Place and Duration of Study:** Department of Physics, Marwari College under University Department of Physics, T.M.B.U. Bhagalpur between January 2014 and June 2014.

**Methodology:** It is completely theoretical based work using Laptop done at Marwari College Bhagalpur and the residential research chamber of the first author.

**Results:** The astrophysical objects emitting the radiations of frequencies (8.092x10<sup>2</sup>Hz to

<sup>\*</sup>Corresponding author: E-mail: dipomahto@hotmail.com;

 $2.023 \times 10^2$ Hz) or wavelengths  $(3.707 \times 10^5$ m to  $14.828 \times 10^5$ m) in X-ray binaries and frequencies  $(4.046 \times 10^{-3}$ Hz to  $0.809 \times 10^{-6}$ Hz) or wavelengths  $(7.414 \times 10^{10}$ m to  $37.070 \times 10^{13}$ m) in active galactic nuclei may be classified as non-spinning black holes. **Conclusion:** The frequencies or wavelengths of Hawking radiation emitted from non-spinning black holes may be regarded as the characteristics of black holes in addition to the mass, spin and charge.

Keywords: Radius of event horizon; XRBs and AGN.

# **1. INTRODUCTION**

Black holes are mainly characterized by mass, angular momentum (spin) and electric charge. A black hole with no spin or charge is called a "Schwarzschild" black hole. If it has spin, then it is a "Kerr black hole, and if it has electric charge, it is a "Reissner-Nordström" black hole. A black hole with both spin and charge is a "Kerr-Newman" black hole. A stationary black hole is parameterized by just a few number: mass, electric charge and angular momentum (and magnetic monopole charge, except its actual existence in nature has not been demonstrated yet) [1,2]. Kanak Kumari et al. [3] used the Schwarzschild radius to characterize the non-spinning and spinning black holes in addition to the mass, spin and charge. In classical theory, black holes can only absorb and not emit particles. However, it is shown that quantum mechanical effects cause black holes to create and emit particles as if

they were hot bodies with temperature  $\frac{h\kappa}{2\pi k} \approx 10^{-6} \left(\frac{M_{\perp}}{M}\right) \kappa$ , where  $\kappa$  is surface gravity of

black holes and k is the Boltzmann constant [4], but according to the general theory of relativity: A black hole is a solution of Einstein's gravitational field equations in the absence of matter that describes the space time around a gravitationally collapsed star. Its gravitational pull is so strong that even light cannot escape from it [5,6,7].

In this present research paper, we have derived an expression for the wavelength and frequency of Hawking radiation emitted by non-spinning black holes in terms of the radius of event horizon, which may be regarded as the characteristics of non-spinning black holes in addition to mass, spin, charge, Schwarzschild radius etc.

# 2. MASS OF BLACK HOLES

There are some astrophysical objects in universe with masses greater than 3M, the likely maximum mass of a neutron star identified as "black hole candidates". Some of the candidates have masses  $\sim 5 - 20M$  in XRBs and some have masses  $\sim 10^6$ - $10^{9.5}$ M in AGN. Today about 20 excellent black hole candidates are known in XRBs. The following two equations (1) and (2) are used to measure the mass of black hole [8].

$$M = \frac{v^2 r}{G} = \frac{4\pi^2 r^3}{GP_{orbit}^2} = \frac{v^3 P_{orbit}}{2\pi G}$$
(1)

where  $P_{orbit}$  = Period of the orbit, v = Velocity of test particle and r = Radius of the orbit to be valid, provided that r is taken to be semi major axis of the elliptical orbit of the test particle.

British Journal of Applied Science & Technology, 4(29): 4136-4147, 2014

$$f(M) = \frac{M \sin^3 i}{\frac{M_c}{(1+M)^2}}$$
(2)

where f(M) = Mass function, itself greater than  $3M_i M = Mass$  of the black hole candidate,  $M_c = Mass$  of companion star and i = Inclination of the binary orbit.

#### 3. MEASUREMENT OF SPIN (a)

The spin of black hole can be determined by the following equation [9].

$$a_* = \frac{M^2}{J} \tag{3}$$

where M and J are the mass & angular momentum of black hole respectively.

When considering circular orbits in black hole space time, a key concept of  $R_{ISCO}$  was designated for the inner most stable circular orbit. The circular orbits with radii R  $R_{ISCO}$  are stable to small perturbations, whereas  $R < R_{ISCO}$  are unstable. For maximally spinning black hole,  $R_{ISCO} = GM/c^2$ , if the orbit co-rotates with the black hole (a= + 1) and  $R_{ISCO} = 9GM/c^2$ , if the orbit counter-rotates (a= - 1). For non-spinning black hole (a = 0),  $R_{ISCO} = 6GM/c^2$  [8].

#### 4. CHARGE OF BLACK HOLES

For external solution of Reissner-Nordstrom black hole, the mass and charge of nonspinning black holes are the same [10]. There is no horizon, when  $M \ge Q$  [11]. Actually an astro-physical object like black hole is not likely to have any significant electric charge, because it will usually be rapidly neutralized by surrounding plasma. Therefore, black hole can be fully characterized by measuring just two parameters M and a [8].

#### 5. FREQUENCY/WAVELENGTH OF NON-SPINNING BLACK HOLES

On the basis of quantum mechanics, the empty space is not empty at all. In this empty space, there are always particle flashing in to existence and disappear again. They always come in pairs; one particle and one anti-particle, like an electron and a positron, or a photon and another photon with opposite spin and impulse. These particles are called virtual particles. If one virtual particle falls into the black hole and the other escapes as Hawking radiation from black hole. The energy of radiated photons is given by the following equation [7].

$$E = h\nu \tag{4}$$

The energy of a photon of Hawking radiation is given by the following equation (Hawking radiation, htt://library.thinkquest.org/c007571/English/printcore.htm, 2011)

$$E = \frac{hc^3}{16\pi GM} \tag{5}$$

4138

From equation (4) and (5), we have

$$\nu = \frac{c^3}{16\pi GM} \tag{6}$$

All the terms like gravitational constant (G), Planck constant (h) and velocity of light(c) in right hand side of equation (6) are constant except mass (M) of the black hole. These constants have vital role discussed in the research paper [5]. The frequency of radiation is given by

$$V = \frac{c}{\lambda} \tag{7}$$

From equations (6) and (7), we have

$$\lambda = 8\pi \frac{2GM}{c^2} \tag{8}$$

For non-spinning black holes, the radius of event horizon is given by [8].

$$R_s = \frac{2GM}{c^2} \tag{9}$$

Putting the value of equation (9) into equation (8), we have

$$\lambda = 8\pi R_s \tag{10}$$

From equation (7), we have

$$v = \frac{c}{8\pi R_s} \tag{11}$$

Multiplying  $eq^{n}(10)$  and (11), we have

 $v\lambda = c$ (12)

$$\nu \propto \frac{1}{\lambda}$$
 (13)

The relation (11) shows that the frequency of Hawking radiation emitted by the black holes is inversely proportional to the radius of event horizon of black holes where as from relation (10) it is clear that the wavelength of Hawking radiation emitted by the black holes is directly proportional to the radius of event horizon of the black holes. This means that heavier black holes will emit the Hawking radiation of lower frequency or longer wavelength and vice-versa.

The relation (13) shows that the frequency of Hawking radiation emitted by the black holes is inversely proportional to the wavelength which is universal law.

### 6. DATA IN SUPPORT OF SCHWARZSCHILD RADIUS/RADIUS OF THE EVENT HORIZON OF BLACK HOLES

There are two categories of black holes classified on the basis of their masses clearly very distinct from each other, with very different masses  $M \sim 5 - 20 M_{\odot}$  for stellar – mass black holes in X-ray binaries and  $M \sim 10^6 - 10^{9.5} M_{\odot}$  for super massive black holes in galactic nuclei [6,8]. The Schwarzschild radius/radius of the event horizon of non-spinning black holes corresponding to the masses  $M \sim 5 - 20 M_{\odot}$  for stellar – mass black holes in X-ray binaries are 14750 metre to 59000 metre and for the masses  $M \sim 10^6 - 10^{9.5} M_{\odot}$  in super massive black holes in the active galactic nuclei are 2.950x10<sup>9</sup> metre to 1.475x10<sup>13</sup> metre [12].

S. no.	Mass of	$\mathbf{p}$	Wavelength	Frequency
	$BH_s$	$R_s = 2950 \frac{M_{\odot}}{M_{\odot}}$	$\lambda = 8\pi R_s$ metre	$v = \frac{c}{c}$ Hz
	(M)	(in metre)		$8\pi R_s$
1	5M₀	14750	3.707x10 <sup>5</sup> _	8.092x10 <sup>2</sup>
2	$6  M_{\odot}$	17700	4.448 x10 <sup>5</sup>	6.744 x10 <sup>2</sup>
3	$7 \text{ M}_{\odot}$	20650	5.189 x10⁵	5.781 x10 <sup>2</sup>
4	$8 \text{ M}_{\odot}$	23600	5.913 x10⁵	5.073 x10 <sup>2</sup>
5	$9 M_{\odot}$	26550	6.672 x10 <sup>5</sup>	4.496 x10 <sup>2</sup>
6	10 M₀	29500	7.414 x10 <sup>5</sup>	4.046 x10 <sup>2</sup>
7	11 M₀	32450	8.155 x10⁵	3.678 x10 <sup>2</sup>
8	$12 M_{\odot}$	35400	8.996 x10⁵	3.334 x10 <sup>2</sup>
9	13 M₀	38350	9.638 x10⁵	3.112 x10 <sup>2</sup>
10	14 M₀	41300	10.379 x10⁵	2.890 x10 <sup>2</sup>
11	15 M₀	44250	11.121 x10 <sup>5</sup>	2.697 x10 <sup>2</sup>
12	16 M₀	47200	11.862 x10⁵	2.529 x10 <sup>2</sup>
13	17 M₀	50150	12.604 x10⁵	2.380 x10 <sup>2</sup>
14	18 M₀	53100	13.345 x10⁵	2.248 x10 <sup>2</sup>
15	19 M <sub>⊙</sub>	56050	14.086 x10 <sup>5</sup>	2.129 x10 <sup>2</sup>
16	20 M <sub>o</sub>	59000	14.828 x10⁵	2.023 x10 <sup>2</sup>

		<i>.</i>		
Table 1. Wavelength	and frequenc	y of non-spinnin	g black holes	S IN XRBS

S. no.	Mass of	$R = 2950 \frac{M}{M}$	$R_{s}$	$\lambda = 8\pi R_s$		с С	$Mod \log(v)$
	$BH_{s}$ (M)	$M_{s} = 2550 M_{\perp}$	log(°)	(in metre)	$\log(\lambda)$	$V = \frac{1}{8\pi R_s}$	
	( )	(in metre)				3 <b>HZ</b>	
1	$1  ext{ x } 10^{\circ}  ext{ M}_{\odot}$	2.950 x10 <sup>°</sup>	9.4698	$7.414 \times 10^{10}$	10.8700	$4.046 \times 10^{-3}$	3.6070
2	2 x 10 <sup>6</sup> M <sub>☉</sub>	5.950 x10 <sup>9</sup>	9.7709	$14.953 \times 10^{10}$	11.1747	$2.006 \times 10^{-3}$	3.3023
3	$3  ext{ x } 10^{6}  ext{ M}_{\odot}$	8.850 x 10 <sup>9</sup>	9.9469	$22.242 \times 10^{10}$	11.3471	$1.348 \times 10^{-3}$	3.1296
4	$4  ext{ x } 10^6  ext{ M}_{\odot}$	1.180x10 <sup>10</sup>	10.0719	$29.656 \times 10^{10}$	11.4721	$1.011 \times 10^{-3}$	3.0047
5	$5  ext{ x } 10^6  ext{ M}_{\odot}$	1.475x10 <sup>10</sup>	10.1688	$37.070 \times 10^{10}$	11.5690	$0.809 \times 10^{-3}$	3.0920
6	$6  ext{ x } 10^6  ext{ M}_{\odot}$	1.770x10 <sup>10</sup>	10.2480	$44.448 \times 10^{10}$	11.6478	$0.674 \times 10^{-3}$	3.1713
7	$7  ext{ x } 10^6  ext{ M}_{\odot}$	2.065x10 <sup>10</sup>	10.3149	$51.899 \times 10^{10}$	11.7151	$0.578 \times 10^{-3}$	3.2380
8	$8  ext{ x } 10^6  ext{ M}_{\odot}$	2.360x10 <sup>10</sup>	10.3729	$59.313 \times 10^{10}$	11.7731	$0.505 \times 10^{-3}$	3.2967
9	$9  ext{ x } 10^6  ext{ M}_{\odot}$	2.655x10 <sup>10</sup>	10.4241	$66.727 \times 10^{10}$	11.8243	$0.449 \times 10^{-3}$	3.3477
10	$1  ext{ x } 10^7  ext{ M}_{\odot}$	2.950x10 <sup>10</sup>	10.4698	$7.414 \times 10^{11}$	11.8700	$4.046 \times 10^{-4}$	4.6070
11	$2  ext{ x } 10^7  ext{ M}_{\odot}$	5.950x10 <sup>10</sup>	10.7709	$14.953 \times 10^{11}$	12.1747	$2.006 \times 10^{-4}$	4.3023
12	$3  ext{ x } 10^7  ext{ M}_{\odot}$	8.850x10 <sup>10</sup>	10.9469	$22.242 \times 10^{11}$	12.3471	$1.348 \times 10^{-4}$	4.1296
13	$4  ext{ x } 10^7  ext{ M}_{\odot}$	1.180x10 <sup>11</sup>	11.0719	$29.656 \times 10^{11}$	12.4721	$1.011 \times 10^{-4}$	4.0047
14	$5  ext{ x } 10^7  ext{ M}_{\odot}$	1.475x10 <sup>11</sup>	11.1688	$37.070 \times 10^{11}$	12.5690	$0.809 \times 10^{-4}$	4.0920
15	$6  ext{ x } 10^7  ext{ M}_{\odot}$	1.770x10 <sup>11</sup>	11.2480	$44.448 \times 10^{11}$	12.6478	$0.674 \times 10^{-4}$	4.1713
16	$7  ext{ x } 10^7  ext{ M}_{\odot}$	2.065x10 <sup>11</sup>	11.3149	$51.899 \times 10^{11}$	12.7151	$0.578 \times 10^{-4}$	4.2380
17	$8  ext{x} 10^7  ext{ M}_{\odot}$	2.360x10 <sup>11</sup>	11.3729	59.313×10 <sup>11</sup>	12.7731	$0.505 \times 10^{-4}$	4.2967
18	$9  ext{ x } 10^7  ext{ M}_{\odot}$	2.655x10 <sup>11</sup>	11.4241	$66.727 \times 10^{11}$	12.8243	$0.449 \times 10^{-4}$	4.3477
19	$1  ext{ x } 10^8  ext{ M}_{\odot}$	2.950x10 <sup>11</sup>	11.4698	$7.414 \times 10^{12}$	12.8700	$4.046 \times 10^{-5}$	5.6070
20	$2  ext{ x } 10^8  ext{ M}_{\odot}$	5.950x10 <sup>11</sup>	11.7709	$14.953 \times 10^{12}$	13.1747	$2.006 \times 10^{-5}$	5.3023

Table 2. Wavelength and frequency of non-spinning black holes in AGN

British Journal of Applied Science & Technology, 4(29): 4136-4147, 2014

Table 2 continued							
21	3 x 10 <sup>8</sup> M <sub>☉</sub>	8.850x10 <sup>11</sup>	11.9469	$22.242 \times 10^{12}$	13.3471	$1.348 \times 10^{-5}$	5.1296
22	$4  ext{ x } 10^8  ext{ M}_{\odot}$	1.180x10 <sup>12</sup>	12.0719	$29.656 \times 10^{12}$	13.4721	$1.011 \times 10^{-5}$	5.0047
23	$5  ext{ x } 10^8  ext{ M}_{\odot}$	1.475x10 <sup>12</sup>	12.1688	$37.070 \times 10^{12}$	13.5690	$0.809 \times 10^{-5}$	5.0920
24	$6 \times 10^8 M_{\odot}$	1.770x10 <sup>12</sup>	12.2480	$44.448 \times 10^{12}$	13.6478	$0.674 \times 10^{-5}$	5.1713
25	$7  ext{ x } 10^8  ext{ M}_{\odot}$	2.065x10 <sup>12</sup>	12.3149	$51.899 \times 10^{12}$	13.7151	$0.578 \times 10^{-5}$	5.2380
26	8 x 10 <sup>8</sup> M <sub>☉</sub>	2.360x10 <sup>12</sup>	12.3729	59.313×10 <sup>12</sup>	13.7731	$0.505 \times 10^{-5}$	5.2967
27	9 x 10 <sup>8</sup> M <sub>☉</sub>	2.655x10 <sup>12</sup>	12.4241	$66.727 \times 10^{12}$	13.8243	$0.449 \times 10^{-5}$	5.3477
28	1 x 10 <sup>9</sup> M <sub>☉</sub>	2.950x10 <sup>12</sup>	12.4698	$7.414 \times 10^{13}$	13.8700	$4.046 \times 10^{-6}$	6.6070
29	2 x 10 <sup>9</sup> M <sub>☉</sub>	5.950x10 <sup>12</sup>	12.7709	$14.953 \times 10^{13}$	14.1747	$2.006 \times 10^{-6}$	6.3023
30	3 x 10 <sup>9</sup> M <sub>☉</sub>	8.850x10 <sup>12</sup>	12.9469	$22.242 \times 10^{13}$	14.3471	$1.348 \times 10^{-6}$	6.1296
31	$4  ext{ x } 10^9  ext{ M}_{\odot}$	1.180x10 <sup>13</sup>	13.0719	$29.656 \times 10^{13}$	14.4721	$1.011 \times 10^{-6}$	6.0047
32	5 x 10 <sup>9</sup> M <sub>☉</sub>	1.475x10 <sup>13</sup>	13.1688	$37.070 \times 10^{13}$	14.5690	$0.809 \times 10^{-6}$	6.0920

# 7. RESULTS AND DISCUSSION

In the present paper, we have derived an expression for the wavelength and frequency of Hawking radiation emitted by black holes in terms of the radius of event horizon using the energy of radiated photons of black holes ( $E = h\nu$ ), the energy of a photon of Hawking

radiation (  $E = \frac{hc^3}{16\pi GM}$  ) and the radius of event horizon of the non-spinning black holes

 $(R_s = \frac{2GM}{c^2})$  with proper mathematical operation. From the Tables 1 and 2, it is clear that

the radiations emitted by black holes are within the range of frequencies from  $8.092 \times 10^{2}$ Hz to  $2.023 \times 10^{2}$ Hz or wavelengths from  $3.707 \times 10^{5}$  m to  $14.828 \times 10^{5}$ m in X-ray binaries and frequencies from  $4.046 \times 10^{-3}$  Hz to  $0.809 \times 10^{-6}$  Hz or wavelengths from  $7.414 \times 10^{10}$  m to  $37.070 \times 10^{13}$  m in active galactic nuclei. The observations from the Tables 1 and 2, it is also clear that the wavelength of radiations emitted by black holes increases with increase the radius of event horizon of the non-spinning black holes and vice-versa in the case of XRBs as well as AGN, but the frequency of radiations emitted by black holes. These two parameters like wavelength and frequency may be regarded as the characteristics of black holes in addition to the mass, spin and charge, because other characteristics the non-spinning black holes can be estimated with the help wavelength and frequency. Hence it may say that the astrophysical objects emitting the radiations of frequencies ( $8.092 \times 10^{2}$ Hz to  $2.023 \times 10^{2}$ Hz) or wavelengths ( $3.707 \times 10^{5}$  m to  $14.828 \times 10^{5}$ m) in X-ray binaries and frequencies ( $4.046 \times 10^{-3}$ Hz to  $0.809 \times 10^{-6}$ Hz) or wavelengths ( $7.414 \times 10^{10}$  m to  $37.070 \times 10^{13}$  m) in active galactic nuclei may be characterized as non-spinning black holes.

The graphs have been plotted between

- I. the radius of event horizon ( $R_s$ ) of different black holes and their corresponding wavelength in XRBs (Fig. 1)
- II. the radius of event horizon ( $R_s$ ) of different black holes and their corresponding frequency in XRBs (Fig. 2)
- III. the radius of event horizon ( $R_s$ ) of different black holes and their corresponding wavelength in AGN (Fig. 3).
- IV. the radius of event horizon ( $R_s$ ) of different black holes and their corresponding frequency in AGN (Fig. 4).

Figs. 1 and 3 obtained for XRBs and AGN in the case of the radius of event horizon verses corresponding wavelength of non-spinning black holes are in a straight line showing that there is a uniform variation between the radius of event horizon and their corresponding wavelength of non-spinning black holes. The straight line also shows that there is a linear relationship between the radius of event horizon and wavelength of non-spinning black holes and justifies the validity of model ( $\lambda = 8\pi R_s$ ), while in the case of XRBs, the graph 2 plotted between radius of event horizon and their corresponding frequency of non-spinning black holes shows that the frequency decreases gradually with increase of the radius of event horizon.

From the Table 2, it is clear that the frequency of Hawking radiation emitted from nonspinning black holes decreases with the increase of mass/radius of the event horizon of the non-spinning black holes in peculiar nature as shown in the graph 4 for AGN. In fact the frequency of Hawking radiation emitted from non-spinning black holes in AGN is so small that they are not easily detectable. In the logarithmic scale, the negative values are obtained, so their modes are taken into consideration for our convenience. From the observation of graph 4, we find that the black holes are categorized for the same order of mass or radius of event horizon which follow the same character. The non-spinning black holes of mass (1 x  $10^6 M_{\odot}$ , 1 x  $10^7 M_{\odot}$ , 1 x  $10^8 M_{\odot}$ , 1 x  $10^9 M_{\odot}$ ), (2 x  $10^6 M_{\odot}$ , 2 x  $10^7 M_{\odot}$ , 2 x  $10^8 M_{\odot}$ , 2 x  $10^9 M_{\odot}$ ) M<sub>o</sub>), (3 x  $10^6 M_{\odot}$ , 3 x  $10^7 M_{\odot}$ , 3 x  $10^8 M_{\odot}$ , 3 x  $10^9 M_{\odot}$ ) and (rest non-spinning black holes in AGN from Table 2) are in four categories. If we plot the graphs for each category in the same graph paper, four parallel lines can be obtained.



Fig. 1. The graph plotted between the radius of event horizon and wavelength of the different test non- spinning black holes in X-ray binaries (XRBs)

British Journal of Applied Science & Technology, 4(29): 4136-4147, 2014



Fig. 2. The graph plotted between the radius of event horizon and frequency of the different test non- spinning black holes in X-ray binaries (XRBs)



Fig. 3. The graph plotted between the radius of event horizon and wavelength of the different test non- spinning black holes in Active Galactic Nuclei (AGN)



# Fig. 4. The graph plotted between the radius of event horizon and frequency of the different test non- spinning black holes in Active Galactic Nuclei (AGN)

# 8. CONCLUSION

In the present work, we can draw the following conclusions:

- The Hawking radiation emitted by the black holes may be regarded as the characteristics of non-spinning black holes in terms of wavelength or frequency.
- The frequencies of the Hawking radiation emitted by the non-spinning black hole decreases with the increase of the mass of different test non-spinning black holes.
- The wavelength of the Hawking radiation increases with the increase of the mass of different test non-spinning black holes.
- The graph plotted between the radius of event horizon verses corresponding wavelength of non-spinning black holes is in a straight line showing that there is a uniform variation between them in XRBs and AGN.
- The graph plotted between radius of event horizon and their corresponding frequency of non-spinning black holes in the case of XRBs shows that the frequency decreases gradually with increase of the radius of event horizon, while likely wave nature variation in AGN.
- A group of black holes having exactly the same order of mass follow the same character.

### ACKNOWLEDGEMENTS

Authors are also grateful to the referee for pointing out the technical errors in the original manuscript and making constructive suggestions.

# **COMPETING INTERESTS**

Authors have declared that no competing interests exist.

# REFERENCES

- 1. Ruffini R, Wheeler JA. Introducing the black hole. Physics Today. 1971;24(12):30-41.
- 2. Mahto D, Kumari K, Sah RK, Singh KM. Study of non-spinning black holes with reference to the change in energy and entropy. Astrophys Space Science. 2012;337(2):685-691.
- 3. Kumari K, Mahto D, Chandra G, Kumar PK. Study of black holes with reference to characterizing parameters. Acta Ciencia Indica. 2012;38(1):67-70.
- 4. Hawking SW. Particle creation by black holes. Communications in Mathematical Physics. 1975;43(3):199-220.
- 5. Dabholkar A. Black hole entropy in string theory-a window in to the quantum structure of gravity. Current Science. 2005;89(12):25.
- 6. Mahto D, Prakash V, Singh BK, Singh KM. Change in entropy of Non-spinning black holes w.r.t. the radius of event horizon in XRBs. Astrophys Space Science. 2012;343(1):153-159.
- 7. Mahto D, Jha BK, Singh KM, Parhi K. Frequency of Hawking radiation from black holes. International Journal of Astrophysics and Space Science. 2013;1(4):45-51.
- 8. Narayan R. Black Holes in Astrophysics, New Journal Physics. 2005;7(1):1-31.
- 9. Mahto D, Kumari A, Singh KM. Energy and entropy change of spinning black holes. International Journal of Engineering and Innovative Technology. 2013;3(5):270-273.
- 10. Chappell I. Overcharging and over spinning a Black Hole. Available: http://www.physics.umd.edu/grt/taj776/chppell.pdf.
- 11. Transchen J. An introduction to black hole evaporation; 2000, arXiv: gr-qc/0010055vi.
- 12. Mahto D, Mehta RN, Parhi K, Sah RK. Energy of non-spinning black holes in XRBs and AGN. Scientific Journal of Physical Science. 2013;3(2):1-5.

© 2014 Mahto et al.; This is an Open Access article distributed under the terms of the Creative Commons Attribution License (http://creativecommons.org/licenses/by/3.0), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Peer-review history:

The peer review history for this paper can be accessed here: http://www.sciencedomain.org/review-history.php?iid=621&id=5&aid=5603