



# *Article* **Dynamic Response of Structurally Reinforced Wing Leading Edge against Soft Impact**

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**Abstract:** In this current research, a commercial aircraft metallic leading edge structurally reinforced with a Y-shaped and V-shaped plate system is numerically examined to investigate the effectiveness of such reinforcements against soft impacts, more commonly known as bird strikes in the aviation industry. A non-linear finite element code Ansys Explicit is adopted to run the virtual test cases. The computational bird model is presented with the Lagrange algorithm and Mooney–Rivlin hyperelastic material parameters which are validated against the experimental data found in the literature. A second validation of the leading edge deformation pattern is also carried out to ensure the accuracy of the present work. Numerical outcomes suggest that due to the presence of the reinforcement, the leading edge skin is restrained from being drastically deformed and the bird model tears apart into two pieces requiring the leading edge model to absorb much less kinetic energy. Additionally, it is found that both the reinforcements have similar crashworthiness performance against bird impacts. The novelty of the research lies in founding the structural reinforcement as a primary preference to strengthen the vulnerable wing leading edge during bird impacts.

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**Keywords:** bird strike; soft impact; structural reinforcement; metallic leading edge; explicit dynamics; lagrange bird model

## **1. Introduction**

Foreign objective debris (FOD) poses a great threat to the aviation industry. According to the US Department of Transportation, FOD is defined as a living or non-living object which is inappropriately located in the airport environment and has the potential to damage both fixed and rotary-wing aircraft [\[1\]](#page-11-0). However, 90% of FOD is attributed to avian creatures, more specifically, different species of birds [\[2\]](#page-11-1), and the collision between a bird and the aircraft is widely known as bird strike, which causes death to the bird and minor to major damage to the impacted structure. As for the aircraft structure, several parts are identified to be more prone to bird impacts than others. For instance, engine fan blades and aircraft wing leading edges account for 44% and 31% of impact cases, which are significantly higher than fuselage (4%), windshield (13%), and radome (8%) [\[3\]](#page-11-2). However, to ensure safe flight operation, all the above-mentioned parts require certification against bird strikes from authorized organizations like the Federal Aviation Administration, European Aviation Safety Agency, Civil Aviation Administration of China, etc.

Due to the emergence of modern powerful workstations, it is now possible to identify the potential material and structure against bird impacts well in advance, before manufacturing the aircraft components which eventually reduces the production time and experimental costs. Nonetheless, before the progress of the computational era, analytical solutions and experimental data were the main means of calculating pressure exerted by the birds on both rigid and deformable plates [\[4](#page-11-3)[,5\]](#page-11-4) which hold their value till today. To gain confidence in adopting commercial software code for bird strike case studies, collaborative

research between the academy and industry is carried out by Guida et al. [\[6–](#page-11-5)[8\]](#page-11-6) on the tailplane leading edge made of composite material and fiber metal laminates. They found a good correlation between the experimental and numerical data to ensure the validity of numerical codes as an alternative solution to bird strike problems. A similar conclusion is

also drawn by Georgiadis et al. [\[9\]](#page-11-7) after completing a series of experimental and numerical investigations on the Boeing 787 composite moveable trailing edge structure. Further successful numerical validations of bird strike events on aircraft structure can be found in references [\[10,](#page-11-8)[11\]](#page-11-9).

Grimaldi et al. [\[12\]](#page-11-10) investigated bird strikes on windshield structures and found that impact angle plays a crucial role in the absorbed energy of the structure. Furthermore, Zhang et al. [\[13\]](#page-11-11) studied the attitude angle of bird impacts on the engine fan blade and concluded that with increasing attitude angle, the peak force becomes larger and at an angle of 90◦ , the blade becomes most vulnerable. Badshah et al. [\[14\]](#page-11-12) numerically calculated the critical frequencies and excitation revolution per minute (RPMs) of an engine rotor and suggested that it is crucial to consider the blade-off condition generated due to bird strike events to avoid the engine working on a critical RPM. A similar study on the rotation of engine fan blades concluded that during the higher rotational speed, the damage is greater due to the impact [\[15\]](#page-11-13). More recently, Zhou et al. [\[16\]](#page-11-14) computationally examined the damage maps of square composite laminates and revealed that changing the ply angle from 0° to 45° leads to a change of damage from globally distributed to a more locally distributed pattern. In another study, the same authors concluded that despite having significantly different damage contours during bird impacts, composite materials reinforced with same fibers have minor effects on the bird deformation [\[17\]](#page-11-15). A brief overview of the composite damage modeling during bird impacts can be found in the literature [\[18,](#page-11-16)[19\]](#page-11-17). Taking consideration of the temperature, a study on heated fiber glare laminate suggests that thermal conditioning at  $85^\circ$  for 45 min restricts the damage of the plate with the support of resin plasticization [\[20\]](#page-11-18).

Several crucial efforts are being made to improve the dynamic response of the leading edge structure against bird impacts. Reglero et al. [\[21\]](#page-11-19) reinforced the leading edge with aluminum foam and found that the composite structure exhibits four times better global deformation than the original one. Later on, Liu et al. [\[22\]](#page-11-20) suggested a novel triangular reinforcement component to improve the anti-bird strike performance of a tail leading edge. He concluded that the reinforcement can reduce the deformation and damage of the leading edge significantly. Qiu et al. [\[23\]](#page-12-0) numerically studied the leading edge honeycomb structure and suggested that beam reinforcement under the sandwich panel can avoid breakdown during a bird impact. More recently, an investigation conducted by Yu et al. [\[24\]](#page-12-1) concluded that localized strengthened variable-thickness skin (LSVTS) can protect the leading edge skin from being penetrated by the bird. Furthermore, Caprio et al. [\[25\]](#page-12-2) analyzed the influence of skin parameters, namely, inner and outer face thickness, and the height of the honeycomb core on the crashworthiness performance of the leading edge. He concluded that to improve the structural performance of the leading edge with minimal weight increment, it is best to increase the height of the honeycomb core. On the contrary, increasing the thickness of the faces leads to a significant weight increment and less damage prevention. A similar study on the honeycomb sandwich panel with bi-layer Ceramic (B4C)/Aluminum (Al7075-T6) facesheets reveals that together they can significantly improve the impact damage produced by the meteoroid orbital debris, by combining the brittle fracture of ceramics layer and large bulge due to plasticization of aluminum layer [\[26\]](#page-12-3).

As for the concern of the bird geometry, Meguid et al. [\[27\]](#page-12-4) studied three different standard bird geometries, namely, (a) cylindrical with straight-end, (b) cylindrical with hemispherical-end, and (c) ellipsoidal, and found that the contact area between the bird and target during the early phase of the impact has a crucial effect on the peak impact force value. In addition to the bird geometry, four different modeling techniques, namely, Lagrange (LE), Euler, Arbitrary Lagrange Euler (ALE), and Smoothed Particle Hydrodynamics (SPH) can be adapted to represent the computational bird model [\[28\]](#page-12-5). Despite having advantages and disadvantages of the models, most modern-day researchers rely on the SPH method which generally provides better accuracy with real impact phenomena in comparison to other solvers [\[29\]](#page-12-6). Considering 90% of the bird body is filled with water, it is quite common to utilize the equation of state (EOS) of water to determine the bird material [\[30\]](#page-12-7). Furthermore, other material models, for instance, the Mooney-Rivlin hyperelastic model of ballistic gelatin and rubber also provide an efficient solution to bird material parameters [\[31\]](#page-12-8). Additional research on the computational bird modeling technique can be found in references [\[32](#page-12-9)[,33\]](#page-12-10).

In summary, a considerable amount of research can be found on finite element validations [\[6](#page-11-5)[–11\]](#page-11-9), response of aircraft structures to bird impacts [\[12](#page-11-10)[–20\]](#page-11-18), and computational representation of birds [\[27](#page-12-4)[–33\]](#page-12-10). However, only in recent times, the emphasis is given towards the improvement of aircraft leading edge structures exposed to bird impacts by means of reinforcements [\[21](#page-11-19)[–26\]](#page-12-3). To determine the convenient reinforcement type, the current research focuses on the potential improvement of a reinforced leading edge by a Y-shaped and V-shaped plate system against bird impact which can be installed on a commercial aircraft. Crashworthiness comparisons are detailed with a leading-edge without the presence of such reinforcements based on the bird strike events, energy absorption, and plastic deformation. Additionally, available literature comparisons are also drawn to demonstrate the effectiveness of such reinforcements over others during bird impacts.

### **2. Test Article Design**

To capture realistic bird impact events, it is important to consider the numerical approaches which should comply with the experimental test articles. Therefore, in this present research, the leading edge along with the test rig is modeled similar to an experimental setup found in the literature [\[25](#page-12-2)[,34\]](#page-12-11), as shown in Figures [1](#page-2-0) and [2,](#page-3-0) apart from the leading edge materials and thickness of the skin, ribs, and reinforcements, which are discussed in the following section. Additionally, the steel NP-360 beam which is mainly used to prevent the bird impact in case of penetration is not modeled since it has no significance to the numerical outcomes. As for the bird geometry, a cylindrical shape with a diameter of 134 mm and a length of 268 mm is selected to keep the standard length-to-diameter ratio of 2:1 which is also the same as the reference.

<span id="page-2-0"></span>

**Figure 1.** Experimental and Numerical Model according to the literature. Reprinted with permission from Refs. [\[25,](#page-12-2)[34\]](#page-12-11). 2020 [\[25\]](#page-12-2) and 2019 [\[34\]](#page-12-11), Di Caprio et al.

<span id="page-3-0"></span>

**Figure 2.** Present Numerical Setup. (**A**) 3D view with sub-components; (**B**) Frontal view; (**C**) Side view.

Next, the investigated structural reinforcement of the Y-shaped plate system and V-shaped plate system is illustrated in Figure [3.](#page-3-1) The skin of the leading edge is assumed to be 2.7 mm thick and made of Aluminum-2024-T3 alloy while the ribs are assumed to be 2.1 mm thick made of Aluminum-7075-T6 alloy. The thickness of the Y-shaped and V-shaped plate systems are kept as 2.4 mm made of Aluminum-7075-T6 alloy. Nonetheless, the V-shaped reinforcement weighs 8.7% higher than Y-shaped reinforcement.

<span id="page-3-1"></span>

**Figure 3.** Structurally reinforced anti-bird-strike system. (**A**) V-shaped reinforcement; (**B**) Side view of V-shaped reinforcement; (**C**) Y-shaped reinforcement; (**D**) Side view of Y-shaped reinforcement.

For both types of alloys, the Johnson–Cook Material model is selected which suits best when the stress-strain relationship of materials differ significantly at different strain rates. The flow stress is defined as  $σ = (A + Bε<sup>n</sup>)(1 + C ln ε<sup>*</sup>)(1 – T<sup>*m</sup>)$ , where  $σ, ε, A$ denotes as the equivalent stress, equivalent plastic strain, and yield stress of the material, respectively. Other remaining constants, namely, *B*, *n*, *C* and *m* denote to strain hardening modulus, strain hardening exponent, strain rate constant, and thermal softening exponent (in case of considerable heat generation) [\[35\]](#page-12-12). The parameters used in the numerical solver for Aluminum Alloy-2024-T3 and Aluminum Alloy-7075-T6 can be found in Table [1.](#page-4-0) The upper and lower beam along with the test rigs are assumed to be made of steel 4340 and the properties can be found in Ansys Explicit Library [\[36\]](#page-12-13).



<span id="page-4-0"></span>**Table 1.** Johnson–Cook material parameters of Aluminum alloys [\[35\]](#page-12-12).

Finally, the validation of the present numerical model is illustrated in Figure [4](#page-4-1) against the experimental and numerical findings of the adopted reference. From the figure, it is evident that the permanent deformation pattern of the skin is similar to the experimental and numerical findings of the reference. Additionally, no penetration is found despite the fact that the distance between the tips of the two ribs after permanent deformation is 161 mm (Figure [4B](#page-4-1)) while in the reference this value is approximately 293 mm. This discrepancy can be explained based on the materials used for the experimental test article. In the reference, a honeycomb core is adopted which is 6.35 mm high and has an aluminum 2024-T3 made outer and inner face thickness of 1.4 mm and 0.4 mm, respectively. For the present study, the thickness of the skin is simplified to 2.7 mm without any honeycomb core since the main objective of the research is to study the effectiveness of structural reinforcement on the leading edge while in the reference the honeycomb core is used as reinforcement.

<span id="page-4-1"></span>

**Figure 4.** Post impact permanent deformation. (**A**) Experimental and numerical results from the reference. Reprinted with permission from Refs. [\[25,](#page-12-2)[34\]](#page-12-11). 2020 [\[25\]](#page-12-2) and 2019 [\[34\]](#page-12-11), Di Caprio et al.; (**B**) Present numerical result.

## **3. Bird Material Model**

For the current study, the computational bird model is presented as the Lagrange model with node erosion algorithm, where the highly distorted nodes are removed from the solver after the impact has taken place to stabilize the solution procedure [\[37\]](#page-12-14), as shown

<span id="page-5-0"></span>

**Figure 5.** Eroded nodes after an impact.

<span id="page-5-1"></span>**Table 2.** Bird Material Parameters [\[31\]](#page-12-8).



Both the Lagrange bird model and material parameters are validated against the experimental data found in the literature [\[31](#page-12-8)[,38\]](#page-12-15). In Figure [6A](#page-5-2), central back displacement data of an aluminum plate impacted by a ballistic gelatin bird projectile are experimentally measured by the direct image correlation (DIC) method at an impact velocity of 122 m/s, which is compared with the numerical outcomes adopting Ansys. Furthermore, in Figure [6B](#page-5-2), the maximum central back displacement values at different impact velocities are correlated. From both the graphs, it is evident that the numerical and experimental data are in excellent agreement.

<span id="page-5-2"></span>

**Figure 6.** Post impact displacement data of experimental [\[38\]](#page-12-15) and numerical outcomes. (**A**) Central back displacement at 122 m/s; (**B**) Maximum central back displacement at different impact velocities.

Finally, the radial spread of the gelatine bird projectile captured by a high-speed camera during experimentation and adopting the SPH method is compared with the current numerical bird model, as shown in Figure [7.](#page-6-0) An excellent correlation is observed with illustrations found in the literature [\[38\]](#page-12-15). In summary, it can be concluded that the Lagrange bird model with node erosion algorithm and Mooney–Rivlin material parameters can be successfully adopted as bird model for the current investigation.

in Figure [5.](#page-5-0) Moreover, Mooney–Rivlin material parameters are selected, which can be found in Table [2.](#page-5-1)

<span id="page-6-0"></span>

**Figure 7.** Radial spread of bird model. (**A**) Experimental observation. Reprinted with permission from Ref. [\[38\]](#page-12-15). 2019, Zhou et al.; (**B**) SPH model. Reprinted with permission from Ref. [\[38\]](#page-12-15). 2019, Zhou et al.; (**C**) Current Lagrange model.

#### **4. Numerical Outcomes**

## *4.1. Bird Strike Impact Events*

At first, the impact events are discussed from the computational bird model's point of view, as shown in Figure [8.](#page-7-0) At the beginning of the impact event, to be precise at 0.5 milliseconds, radial deformation of the bird starts to take place and no visual differences among the leading edge models are observed. However, as time progresses, at 1 millisecond, the bird continues to deform radially for the leading edge without any reinforcement while a tendency of splitting the bird into two pieces is observed for both the V-shaped and Y-shaped reinforcement. Afterwards, at 2 milliseconds, the whole bird model is almost split into half while impacting with reinforced leading edges. In contrast, half of the bird is radially deformed for the case of leading edge without any reinforcement. At 3 milliseconds, the split of the bird is fully completed which is more apparent at 4 milliseconds for reinforcements. Nonetheless, deformation continues to take place for the leading edge having no reinforcement and a fully deformed shape of the bird model can be seen after the termination of the solution, completely crashing on the wing surface. Lastly, it is found that for both the reinforcement types, the bird model impact events are identical.

## *4.2. Energy Summary*

Next, energy conversion data of the whole system comprising both the test rig and leading edge with and without reinforcement can be found in Figure [9.](#page-8-0) From the illustration, it is evident that most of the kinetic energy of the bird is converged to internal energy for the case of leading edge without any reinforcement. The maximum internal energy reaches the peak value of 22.62 KJ at 8 ms and stabilizes afterward. However, for the case of reinforcements, a completely different scenario can be observed, where the kinetic energy of the bird decreases from 30.4 KJ to 19 KJ and continues to retain the energy. This phenomenon can be described from the previous illustration (Figure [8\)](#page-7-0) where the bird, after being impacted, is sliced into two pieces due to the presence of the reinforcements. Thus, a full crashing of the bird model does not take place and the specified kinetic energy remains in the bird model. Therefore, the system with reinforcements requires the absorption of less kinetic energy, and the maximum peak values of 7.63 KJ and 7.49 KJ internal energy are produced by V-shaped and Y-shaped reinforcements, respectively, which stabilizes at 2.5 milliseconds. Similar to the previous bird strike events, both reinforcement types exhibit almost identical energy summary, generating approximately 67% less internal energy than the system without reinforcement.

<span id="page-7-0"></span>

**Figure 8.** Bird projectile impact events.

<span id="page-8-0"></span>

**Figure 9.** Energy conversion data during bird strikes.

Detailed maximum energy dissipation by the components can be seen in Table [3.](#page-8-1) In all cases, the skin absorbs the highest amount of internal energy. However, the amount of energy dissipation varies largely due to the presence of reinforcements. The skin generates 17 KJ internal energy when no reinforcement is placed, which is approximately 83% higher than the reinforced skins. Furthermore, the test rig also generates a maximum of 3.1 KJ internal energy, which is around 81% higher in contrast to the V-shaped and Y-shaped reinforced leading-edge installed test rigs. It is also interesting to note that, both the reinforcements generate only a small amount of internal energy, which is only 4% of the total internal energy of the system.

<b>Wing Model</b>	Skin, KJ	Ribs, KI	Reinforcement, KJ	Test Rig, KJ
No reinforcement		0.33	$\overline{\phantom{0}}$	3.1
V-shaped reinforcement	2.8	0.06	0.324	0.61
Y-shaped reinforcement	2.93	0.06	0.3	0.55

<span id="page-8-1"></span>**Table 3.** Maximum internal energy by the components.

Focusing on the plastic work of the skin as illustrated in Figure [10A](#page-9-0), it can be seen that the skin without reinforcement experiences a large plastic deformation. The plastic work done by the skin is around 15.44 KJ which is 68.4% of the internal energy of the skin. In contrast, plastic work of the skin with reinforcements is insignificant, to be specific, only 0.21 KJ and suggests a small area of plastic deformation due to the bird strike events. Furthermore, the test rig installed with the leading edge having no reinforcement carries out 2.05 KJ plastic work which can not be neglected considering the contribution to be around 9% of the total internal energy of the system, as shown in Figure [10B](#page-9-0). On the other hand, the plastic work of the test rigs with reinforced leading edges is considerably low, only around 0.18 KJ.

<span id="page-9-0"></span>

**Figure 10.** Plastic work. (**A**) Skin; (**B**) Test Rig.

## *4.3. Deformed Configuration*

Finally, the permanent deformation of the wing leading edge after the bird impact events can be seen in Figure [11.](#page-9-1) Even though no penetration takes place, large plastic deformation is found for the wing leading edge without reinforcement. The displacement between the two rib tips is measured as 161 mm, which was initially 640 mm before the impact. On the other hand, despite some plastic deformation near the impacted area having been identified, no tip displacement is observed for the leading edge with reinforcements. This confirms that the leading edge will retain its aerodynamic shape after the bird strike, eventually providing a safer flight.

<span id="page-9-1"></span>

**Figure 11.** Permanent deformation of the wing leading edges.

In terms of plastic displacement and tip displacement, a comparison is also made with other available reinforcement types found in the literature [\[24](#page-12-1)[,25,](#page-12-2)[34\]](#page-12-11), as shown in Figure [12.](#page-10-0) From the illustration, it is apparent that despite being reinforced, all other leading edges have a significant plastic deformation and only provide protection for not being penetrated fully due to the impact, complying with the FAR 25.631 regulations. However, the Y-shaped and V-shaped reinforced leading edges not only satisfy the regulations but also ensure a better aerodynamically shaped structure. It is also noteworthy that other reinforcements cannot split the bird into two pieces and have to absorb all the kinetic energy of the bird until it completely gets demolished.

<span id="page-10-0"></span>

**Figure 12.** Comparison of permanent deformation of the wing leading edges with the literature references. (**A**) Best configured leading edge. Reprinted with permission from Ref. [\[24\]](#page-12-1). 2020, Yu. et al.; (**B**) Best configured leading edge. Reprinted with permission from Ref. [\[25\]](#page-12-2). 2020, Di Caprio et al.; (**C**) Best configured leading edge. Reprinted with permission from Ref. [\[34\]](#page-12-11). 2019, Di Caprio et al.; (**D**) Present Y-shaped and V-shaped configuration.

#### **5. Conclusions**

The present work evaluates the crashworthiness performance of two different reinforcements installed in a metallic aircraft wing leading edge under bird strike events and compared with a traditional leading edge having no reinforcement placed on it. Numerical setup and outcomes have been validated against the experimental data adopting both qualitative and quantitative techniques. From the results, it is found that reinforcements aid in splitting the impacted birds into two pieces. Therefore, the leading edge is required to absorb much less kinetic energy, generating 81.53% less internal energy than the leading edge without reinforcement. Among the components, the skin dissipates the maximum amount of energy followed by the test rig. The plastic work done by the skin is 15.4 KJ without reinforcement which is 0.21 KJ for reinforcement variants.

Another important outcome of the study is that the leading edge with reinforcements does not deform drastically. A tip displacement of 73.9% is observed without reinforcement, suggesting a potential aerodynamic shape loss of the structure. Additionally, other reinforcement types found in the literature have tip displacements after being impacted while the leading edge with reinforcement system withstands the bird impact without disturbing the tip location.

It is also interesting to see that both the reinforcement types have similar crashworthiness performance. Even though no weight comparison against internal energy is studied, from the total mass a significant difference of 8.7% is obtained which directs to a comparison study of the reinforcements with further optimized design.

Finally, based on the observations of the crashworthiness factors, it is suggested to adopt the structural reinforcement as the primary choice of reinforcement to the leading edge wing structure to withstand the high velocity shock impacts effectively.

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